

Outline of Lecture

- **Simple Binary Addition and Subtraction**
- **Overflow**
- **Logical operations**

Addition & Subtraction

- Just like in primary school (carry / borrow 1s)

Examples

| | | |
|---------------|---------------|---------------|
| 0101 | 0111 | 1110 |
| + 0001 | - 0110 | - 0101 |
| 0110 | 0001 | 1001 |

- An alternative for subtraction is to add the negated number

Examples

| | | |
|---------------|---------|---------------|
| 0111 | same as | 0111 |
| + 1010 | | - 0110 |
| 10001 | | |

- Since only 4 bits are available, drop the extra bit on the left most.
- In other words, **0111+1010** gives **0001**

Exercise

- Assume 4-bit 2's complement numbers. What are:
 - a) $1001 - 1100 =$
 - b) $1100 - 1001 =$
 - c) $0010 - 1111 =$
 - d) $1100 + 1001 =$
 - e) $1101 + 0101 =$
- Carry out the followings in 5-bit 2's complement additions:
 - f) $5 - 10 =$
 - g) $-4 - 7 =$

Overflow

- The result may be too large for finite computer word. This is called overflow.

For example, adding two n-bit numbers does not always yield an n-bit number

0111

+0001

1000

note that overflow term is some what misleading, it does not mean a carry overflowed

- $7 + 1$ should be 8, but 8 can't be represented using 4 bits.
- Notice the sign bits are inconsistent when an overflow occurs, two positive numbers add to give a negative number.

Overflow

- The overflow conditions for addition and subtraction are listed below:

| Operation | Operand A | Operand B | Result |
|-----------|-----------|-----------|----------|
| A + B | ≥ 0 | ≥ 0 | < 0 |
| A + B | < 0 | < 0 | ≥ 0 |
| A - B | ≥ 0 | < 0 | < 0 |
| A - B | < 0 | ≥ 0 | ≥ 0 |

Detecting Overflow

- No overflow when adding a +ve and a -ve number
- No overflow when signs are the same for subtraction
- Overflow occurs when the value affects the sign:
 - overflow when adding two positives yields a negative
 - adding two negatives gives a positive
 - subtract a negative from a positive and get a negative
 - subtract a positive from a negative and get a negative
- Consider the operations $A + B$, and $A - B$
 - Can overflow occur if B is 0 ?
 - Can overflow occur if A is 0 ?

Exercise

- In which of the followings would overflow occur?

Assume 5 - bit 2's complement numbers.

a) $10011 - 01101$

b) $10010 + 11010$

c) $01001 + 01101$

d) $01100 + 01111$

e) $10000 - 10010$

Effects of Overflow

- **An exception condition occurs and interrupts normal program execution**
 - **Control jumps to predefined address for exception**
 - **Interrupted instruction address is recorded for possible resumption**
- **Details based on software system / language**
 - **example : flight control vs. homework assignment**
- **Don't always want to detect overflow**
 - **new MIPS instructions treating operands as unsigned numbers: `addu`, `addiu`, `subu`, `sltu`, `sltiu`**

Logical Operations

- Bitwise AND and bitwise OR
 - perform and /or bit by bit
- 0001 and 1011 = 0001
- 0001 or 1011 = 1011

Examples

- and \$t0, \$s0, \$s1
 - or \$t0, \$s1, \$s0
 - andi \$t0, \$s0, 32
 - ori \$t0, \$s2, 15
- Also , XOR, NOR , NOT

More Logical Operations

- It is quite useful in many programs to operate on fields and bits within a word.
- One such operations are called *shifts*. They move all the bits in a word to the left or to the right, filling the emptied bits with 0s.
- MIPS has two shift instructions: *shift left logical* (**sll**) and *shift right logical* (**srl**).

```
sll  $10, $16, 8      # left shift the
                        con  tent of $16  by 8 bits and put
                        result in $10
```

- if \$ 16 contains

01001010000000000000011010000000 then

- \$10 will contain

00000000000011010000000000000000

- Note that the 01001010 is lost and the 00000000 is shifted in from nowhere.

More Logical Operations

- Shift right arithmetic (sra)

sra \$10, \$16, 7 # right shift with sign extension

If \$16 contains

010010100000000000000110100001000

then \$10 will contain

00000000100101000000000000011010

Note that the 0001000 is lost

If \$16 contains

110010100000000000000110100001000

then \$10 will contain

11111111100101000000000000011010

It is like dividing the number by 2^7